

## Proof Notebook Problem 3

### The Problems:

1. Show that the square of every integer has remainder 0, 1, or 4 upon division by 8.
2. Show  $\exists x \in \mathbb{R} \forall y \in \mathbb{R} \exists z \in \mathbb{R} (x^y + z = 0)$ .
3. Let  $x$  and  $y$  be odd integers. If the product  $xy$  has remainder 3 upon division by 4, then one of the factors has division 3 upon division by 4.

*Please do not do multiple problems: you should have a clear mind for the peer review.*

*Only use the third problem if you're in a group of three.*

### Due Dates:

Item	Due Date	Method
Draft 1	Friday, September 19 (10pm)	Blackboard
Peer Review 1	Before 2 <sup>nd</sup> draft	On your own – nothing to turn in
Draft 2	Tuesday, September 23	In class
Draft 3	Friday, September 26 (10pm)	Blackboard
Peer Review 2	Before final version	On your own – nothing to turn in
Final Version	Tuesday, September 30	In class

### The peer review process:

1. Schedule a time to meet in pairs or groups of 3. Come to the meeting with draft 1 completed.
2. Person 1 presents their proof on the board; Person 2 analyzes each step:
  1. Is this step intelligible or nonsense?
  2. Does this step say what the Person 1 thinks it says?
  3. Does this step follow from the previous steps?
  4. Is it clear why this step follows?
3. Switch roles and repeat (2).